

This document shows how to write theorems and proofs, The specific example is a theorem about rational numbers:

**Theorem 1.** *If  $q$  is a rational number and  $n$  is an integer, then  $q+n$  is rational.*

*Proof.* We assume that  $q$  is a rational number and  $n$  is an integer, and will show that  $q + n$  must be rational. Since  $q$  is rational, we can write  $q = \frac{a}{b}$  where  $a$  and  $b$  are integers and  $b \neq 0$ . We also observe that  $n = \frac{nb}{b}$ . Therefore

$$q + n = \frac{a + bn}{b}$$

Since integers are closed under addition and multiplication,  $a + bn$  is an integer. Furthermore,  $b$  is a non-zero integer, and so  $\frac{a+bn}{b}$  is a rational number. We have now shown that if  $q$  is a rational number and  $n$  is an integer, that  $q + n$  is rational.  $\square$